



# The Economics of Internet Search

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# Search engine use

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- Search engines are very popular
  - 84% of Internet users have used a search engine
  - 56% of Internet users use search engines on a given day
- They are also highly profitable
  - Revenue comes from selling ads related to queries



# Search engine ads

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- Ads are highly effective due to high relevance
  - But even so, advertising still requires scale
    - 2% of ads might get clicks
    - 2% of clicks might convert
    - So only .4 out a thousand who see an ad actually buy
    - Price per impression or click will not be large
    - But this performance is good compared to conventional advertising!
- Search technology exhibits increasing returns to scale
  - High fixed costs for infrastructure, low marginal costs for serving



# Summary of industry economies

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- Entry costs (at a profitable scale) are large due to fixed costs
- User switching costs are low
  - 56% of search engine users use more than one
- Advertisers follow the eyeballs
  - Place ads wherever there are sufficient users, no exclusivity
- Hence market structure is likely to be
  - A few large search engines in each language/country group
  - Highly contestable market for users
  - No demand-side network effects that drive towards a single supplier so multiple players can co-exist



# What services do search engines provide?

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- Google as yenta (matchmaker)
  - Matches up those seeking info to those having info
  - Matches up buyers with sellers
- Relevant literature
  - Information science: information retrieval
  - Economics: assignment problem



# Brief history of information retrieval

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- Started in 1970s, basically matching terms in query to those in document
- Was pretty mature by 1990s
- DARPA started Text Retrieval Conference
  - Offered training set of query-relevant document pairs
  - Offered challenge set of queries and documents
  - Roughly 30 research teams participated



# Example of IR algorithm

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- Prob(document relevant) = some function of characteristics of document and query
  - E.g., logistic regression  $p_i = X_i \beta$
- Explanatory variables
  - Terms in common
  - Query length
  - Collection size
  - Frequency of occurrence of term in document
  - Frequency of occurrence of term in collection
  - Rarity of term in collection



# The advent of the web

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- By mid-1990s algorithms were very mature
- Then the Web came along
  - IR researchers were slow to react
  - CS researchers were quick to react
- Link structure of Web became new explanatory variable
  - PageRank = measure of how many important sites link to a given site
  - Improved relevance of search results dramatically





- Brin and Page tried to sell algorithm to Yahoo for \$1 million (they wouldn't buy)
- Formed Google with no real idea of how they would make money
- Put a lot of effort into improving algorithm



# Why online business are different

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- Online businesses (Amazon, eBay, Google...) can continually experiment
  - Japanese term: *kaizen* = "continuous improvement"
  - Hard to really do continuously for offline companies
    - Manufacturing
    - Services
  - Very easy to do online
    - Leads to very rapid (and subtle) improvement
    - Learning-by-doing leads to significant competitive advantage



# Business model

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- Ad Auction
  - GoTo's model was to auction search results
  - Changed name to Overture, auctioned ads
  - Google liked the idea of an ad auction and set out to improve on Overture's model
- Original Overture model
  - Rank ads by bids
  - Ads assigned to slots depending on bids
    - Highest bidders get better (higher up) slots
  - High bidder pays what he bid (1<sup>st</sup> price auction)

# Search engine ads

The screenshot shows a Mozilla Firefox browser window with the address bar displaying the URL: <http://www.google.com/search?hl=en&lr=&safe=off&q=rental&btnG=Search>. The search bar contains the word "rental". The search results are displayed in two columns. The left column shows organic search results, and the right column shows sponsored links. The organic results include links for Hertz, Avis, National Car Rental, and Thrifty Car Rental. The sponsored links include Rent.com, Apartment Rentals, eBay, Apartments.com, Apartment Finder, and Snowmass Condo Rentals.

- Ads are shown based on query + keywords
- Ranking of ads based on expected revenue



# Google auction

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- Rank ads by bid x expected clicks
  - Price per click x clicks per impr = price per impression
  - Why this makes sense: revenue = price x quantity
- Each bidder pays price determined by bidder below him
  - Price = minimum price necessary to retain position
  - Motivated by engineering, not economics
- Overture (now owned by Yahoo)
  - Adopted 2<sup>nd</sup> price model
  - Currently moving to improved ranking method



# Alternative ad auction

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- In current model, optimal bid depends on what others are bidding
- Vickrey-Clarke-Groves (VCG) pricing
  - Rank ads in same way
  - Charge each advertiser cost that he imposes on other advertisers
  - Turns out that optimal bid is true value, no matter what others are bidding



# Google and game theory

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- It is fairly straightforward to calculate Nash equilibrium of Google auction
  - Basic principle: in equilibrium each bidder prefers the position he is in to any other position
  - Gives set of inequalities that can be analyzed to describe equilibrium
  - Inequalities can also be inverted to give values as a function of bids



# Implications of analysis

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- Basic result: *incremental cost per click has to be increasing in the click through rate.*
- Why? If incremental cost per click ever decreased, then someone bought expensive clicks and passed up cheap ones.
- Similar to classic competitive pricing
  - Price = marginal cost
  - Marginal cost has to be increasing





# Simple example

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- Suppose all advertisers have same value for click  $v$ 
  - Case 1: Undersold auctions. There are more slots on page than bidders.
  - Case 2: Oversold auctions. There are more bidders than slots on page.
- Reserve price
  - Case 1: The minimum price per click is (say)  $p_m$  ( $\sim$  5 cents).
  - Case 2: Last bidder pays price determined by 1<sup>st</sup> excluded bidder.



# Undersold pages

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- Bidder in each slot must be indifferent to being in last slot

$$(v - p_s)x_s = (v - r)x_m$$

- Or

$$p_s x_s = v(x_s - x_m) + r x_m$$

- Payment for slot s = payment for last position + value of incremental clicks



# Example of undersold case

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- Two slots
  - $x_1 = 100$  clicks
  - $x_2 = 80$  clicks
  - $v=50$
  - $r=.05$
- Solve equation
  - $p_1 100 = .50 \times 20 + .05 \times 80$
  - $p_1 = 14$  cents,  $p_2=5$  cents
  - Revenue =  $.14 \times 100 + .05 \times 80 = \$18$



# Oversold pages

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- Each bidder has to be indifferent between having his slot and not being shown:
- So  $(v - p_s)x_s = 0$   
$$p_s = v$$
- For previous 2-slot example, with 3 bidders,  $p_s = 50$  cents and revenue =  $.50 \times 180 = \$90$
- Revenue takes big jump when advertisers have to compete for slots!



# Number of ads shown

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- Show more ads
  - Pushes revenue up, particularly moving from underold to oversold
- Show more ads
  - Relevancy goes down
  - Users click less in future
- Optimal choice
  - Depends on balancing short run profit against long run goals



# Other form of online ads

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- Contextual ads
  - AdSense puts relevant text ads next to content
  - Advertiser puts some Javascript on page and shares in revenue from ad clicks
- Display ads
  - Advertiser negotiates with publisher for CPM (price) and impressions
  - Ad server (e.g. Doubleclick) serves up ads to pub server
- Ad effectiveness
  - Increase reach
  - Target frequency
  - Privacy issues



# Conclusion

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- Marketing as the new finance
- Availability of real time data allows for fine tuning, constant improvement
- Market prices reflect value
- Quantitative methods are very valuable
- We are just at the beginning...